Supplementary Material for Camera Pose Estimation using Implicit Distortion Models

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1. Overview of Supplementary Material

The supplementary material contains the following:

- Implementation details (Section 2)
- Detailed results from calibration experiment (Table 4)
- Detailed results for the BA experiment (Section 3)
- Evaluation with GT principal point (Section 4)
- Dataset details (Table 1)
- Additional qualitative results (Figure 4)

2. Implementation Details

Neighborhood selection. To construct the residuals in the regularizer, we select the k = 2m closest neighbours symmetrically around each point. To avoid the instability from the denominator vanishing, a minimum distance δr_{min} to the closest neighbor is enforced. Further, since the locally linear assumption fails when the distance between two neighbors is too large, δr_{max} is set to ensure the distance of that falls below a threshold.

Parameters. In our experiments, δr_{min} is set to be 1 px, while δr_{max} is set to be 100 px. The number of neighbors is chosen to be 4 since it provides a good trade-off between redundancy in the fitting and the sparsity pattern. This is evaluated in the ablation study in the main paper.

Outlier filtering. Given an initial pose estimate we propose to filter outliers in a similar fashion as in [1], using a sliding median filter on the computed f_i . Points where f_i deviate significantly from the median of the local neighbourhood (n = 4) are removed. The threshold is set as $k = 3 \times 1.4826$ times the median error, which correspond to the 99.7% confidence interval assuming the deviations are normally distributed.

3. Evaluation of Bundle Adjustment

The proposed bundle adjustment method optimizes a surrogate problem in each iteration to enable use of the Schur complement trick. However, this inner optimization problem does not minimize the true cost. Figure 1 and Figure 2 show the cost across iterations for bundle adjustment with and without groundtruth principal point. One can observe spikes and energy steps due to the imperfection of the approximation, but still, the surrogate problem is a good approximation and the cost for outer iterations converges almost monotonically as shown in the plots.

4. Impact of Estimated Principal Point

For all the experiments in the paper we estimate the principal point by first assuming it is in the center of the image. The principal point is then refined by minimizing the radial reprojection error (see Section 4 in the main paper). For comparison we here show the results using the ground truth principal point (as used in the reference SfM model). See Table 2 and Table 3. Experiments for optimization with estimated principal point are also listed for reference. Similarly, the proposed method consistently outperforms the the Camposeco et al. [1] when ground truth principal point is used. The improvement for estimation of pose for dataset Kazan and Doge Palace using ground truth principal point is significant, which is due to the poor estimation of principal point. In Figure 1 we show the cost across iterations for bundle adjustment using ground truth principal point, and that with estimated principal point can be found in Figure 2. Cumulative reprojection error plots for bundle adjustment with / without groundtruth principal points can be found in Figure 3. Generally, optimizations with groundtruth principal point give better error, and the difference is more significant when the estimation of principal point is less accurate. Empirically we found that the principal point refinement works slightly better if points close to the center are downweighted in the optimization (as the radial reprojection error is very sensitive to principal point shifts for these correspondences).

Checkerboard calib. images	[3]	github.com/ylochman/babelcalib
Doge Palace and Kazan	[4]	<pre>www.maths.lth.se/matematiklth/personal/calle/dataset/dataset.html</pre>
Grossmunster and Kirchenge	[2]	github.com/vlarsson/radialsfm
Aachen Day-Night	[<mark>5,6</mark>]	https://www.visuallocalization.net/datasets/
InLoc	[7]	https://www.visuallocalization.net/datasets/

Table 1. Datasets used in the experimental evaluation and where to obtain them.

			Kirchenge [2] (369)		Grossmunst	ter [2] (373)	Kazan [4] (282)	Doge Palace [4] (241)	
			ϵ_{rot} (deg.)	ϵ_{pos} (cm.)						
Single image	Droposed	w/	0.014	0.4	0.014	0.4	0.005	1.9	0.010	2.4
	Proposed	w/o	0.023	0.6	0.038	0.9	0.386	8.7	0.338	11.7
	Camposeco et al. [1]	w/	0.024	0.8	0.031	3.7	0.007	2.7	0.016	91.1
		w/o	0.027	0.8	0.044	3.8	0.403	19.8	0.364	121.2
Multiple images	Proposed	w/	0.012	0.3	0.016	0.3	0.004	0.4	0.006	0.4
	rioposed	w/o	0.020	0.4	0.036	0.5	0.379	3.4	0.328	3.4
	Composide at al [1]	w/	0.019	0.4	0.027	0.7	0.007	0.6	0.013	0.7
	Camposeco et al. [1]	w/o	0.027	0.8	0.044	3.8	0.403	19.8	0.364	121.2

Table 2. Average rotation error (in degree) and camera position error (in centimeters) with COLMAP reconstruction result as pseudo groundtruth and optimized with / without groundtruth principal point. The number of images for each dataset is shown in the bracket. Single image optimization and multiple images optimization are presented separately and both compared with method proposed in [1]. Error for principal point estimation for Kirchenge, Grossmunster, Kazan and Doge Palace in px are 0.830, 1.361, 16.456 and 15.377 respectively.

References

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		Upgraded (w/o)		Upgra	Upgraded (w/)		djustment (w/o)	Bundle Adjustment (w/)		
		mean	median	mean	median	mean	median	mean	median	
	ϵ_{rot} (deg.)	1.720	0.398	1.449	0.169	1.726	0.403	1.361	0.084	
Kirchenge	ϵ_{pos} (m.)	0.414	0.028	0.424	0.028	0.401	0.026	0.414	0.025	
	ϵ_{proj}^{GT} (px)	2.199	1.630	1.999	1.728	1.469	1.015	1.088	0.857	
	ϵ_{proj}^{est} (px)	1.633	0.955	1.435	1.071	1.294	0.728	0.974	0.712	
	ϵ_{rot} (deg.)	2.322	0.643	1.993	0.284	2.291	0.716	1.782	0.111	
Grossmunster	ϵ_{pos} (m.)	0.990	0.129	1.008	0.129	0.939	0.093	0.929	0.082	
	ϵ_{proj}^{GT} (px)	2.866	2.110	3.223	2.563	1.631	1.325	1.227	0.935	
	ϵ_{proj}^{est} (px)	2.866	2.110	3.015	2.356	1.516	1.075	1.191	0.869	
	ϵ_{rot} (deg.)	0.463	0.463	0.047	0.047	0.403	0.396	0.041	0.042	
Kazan	ϵ_{pos} (m.)	0.053	0.048	0.021	0.018	0.152	0.112	0.015	0.014	
	ϵ_{proj}^{GT} (px)	1.359	1.084	0.923	0.750	0.834	0.682	0.827	0.699	
	ϵ_{proj}^{est} (px)	0.957	0.720	0.708	0.487	0.658	0.488	0.569	0.401	
	ϵ_{rot} (deg.)	0.401	0.393	0.165	0.154	0.324	0.360	0.021	0.019	
Doge Palace	ϵ_{pos} (m.)	0.040	0.033	0.022	0.013	0.107	0.067	0.007	0.005	
	ϵ_{proj}^{GT} (px)	0.914	0.710	0.776	0.589	1.091	0.981	0.681	0.535	
	$\dot{\epsilon_{proj}^{est}}$ (px)	0.893	0.690	0.647	0.436	0.619	0.453	0.558	0.389	

Table 3. BA with implicit distortion model with and without the GT principal point. Table shows the rotation (deg.) and position (m) errors. We also report reprojection errors, both with the GT calib. and estimated. The estimation error for the principal point for Kirchenge, Grossmunster, Kazan and Doge Palace are 8.504, 17.268, 21.522 and 17.487 respectively. Note that here the principal point estimate is taken from the framework of Larsson et al. [2] which does not downweight residuals close to the image center.



Figure 1. Cost across iterations of optimization for bundle adjustment with groundtruth principal point. Optimization stops when the decrease in cost is less than 0.1%. Start of the outer iterations are marked with blue dots.



Figure 2. Cost across iterations of optimization for bundle adjustment without groundtruth principal point. Optimization stops when the decrease in cost is less than 0.1%. Start of the outer iterations are marked with blue dots.



Figure 3. Bundle adjustment with implicit distortion optimized with / without ground truth principal point. Cumulative reprojection errors using GT calib and estimated. Bundle adjustment using groundtruth principal point in general gives better reprojection error. The estimation error for the principal point for Kirchenge, Grossmunster, Kazan and Doge Palace are 8.504, 17.268, 21.522 and 17.487 respectively. Note that here the principal point estimate is taken from the framework of Larsson et al. [2] which does not downweight residuals close to the image center.



Figure 4. Qualitative results of implicit self-calibration. The images were not seen during calibration showing that our calibration does not overfit to the calibration data.

Name		Training images							Test images					
		Proposed			Camposeco et al. [1]			[3]		Proposed		Camposeco et al. [1]		
	N_{img}	ϵ_{rot}	ϵ_{pos}	$<1^{\circ},1\%$	ϵ_{rot}	ϵ_{pos}	$<1^{\circ},1\%$	ϵ^{BC}_{rms}	ϵ_{pp}	ϵ_{rms}	< 1px	ϵ_{rms}	< 1px	
Kalibr														
BF2M2020S23	35+15	0.28	0.28	33/35	0.21	0.86	28/35	0.18	1.57	0.24	15/15	0.51	14/15	
BF5M13720	35+15	0.12	0.09	35/35	0.25	1.92	31/35	0.18	0.45	0.20	15/15	0.66	14/15	
BM2820	35+15	0.15	0.11	35/35	0.18	0.55	33/35	0.18	1.27	0.21	15/15	0.41	15/15	
BM4018S118	35+15	0.08	0.14	35/35	0.33	0.93	24/35	0.24	0.08	0.27	15/15	0.62	15/15	
ENTANIYA	35+15	0.19	0.13	35/35	0.40	0.40	30/35	0.42	0.99	0.52	15/15	1.00	12/15	
EUROC	35+15	0.25	0.47	34/35	0.63	1.39	20/35	0.13	1.51	0.21	15/15	0.48	15/15	
GOPRO	35+15	0.11	0.11	35/35	0.17	0.39	34/35	0.16	0.53	0.54	13/15	0.93	13/15	
TUMVI	35+15	0.20	0.12	35/35	0.29	0.48	31/35	0.16	0.68	0.19	15/15	0.30	15/15	
OCamCalib														
Fisheye1	10+5	0.21	0.13	10/10	0.70	0.43	8/10	0.59	0.97	0.60	5/5	1.12	1/5	
Fisheye190deg	5+3	0.14	0.16	5/5	0.98	0.96	2/5	0.63	0.41	0.63	3/3	0.93	2/3	
Fisheye2	11+5	0.19	0.20	11/11	0.35	0.38	9/11	0.46	0.04	0.46	5/5	0.57	5/5	
GOPR	7+4	0.14	0.15	7/7	0.16	0.20	7/7	1.23	1.34	2.51	0/4	6.82	0/4	
KaidanOmni	11+6	1.21	0.00	2/11	0.78	0.00	11/11	0.56	2.43	0.68	6/6	0.81	6/6	
Ladybug	9+4	1.03	0.57	4/9	0.92	1.89	0/9	0.67	8.56	1.18	3/4	1.70	0/4	
MiniOmni	10+5	0.89	0.00	7/10	0.38	0.03	10/10	0.71	1.90	1.13	4/5	7.60	0/5	
Omni	9+5	0.76	0.67	8/9	0.46	1.05	3/9	0.78	1.16	1.03	2/5	2.93	0/5	
VMRImage	7+3	0.67	0.64	7/7	0.61	0.70	5/7	0.56	2.76	0.60	3/3	0.67	3/3	
ov														
corner ov00	35+15	1.28	0.49	0/35	1.46	0.64	0/35	0.70	20.05	1.34	0/15	2.62	0/15	
corner ov01	35+15	0.61	0.25	35/35	0.71	0.31	35/35	0.71	9.32	0.96	5/15	1.56	0/15	
corner ov02	35+15	1.08	0.80	9/35	1.23	0.58	1/35	2.11	16.16	2.59	1/15	3.48	0/15	
corner ov03	35+15	0.60	0.33	35/35	0.65	0.33	34/35	5.67	9.07	5.82	4/15	6.45	0/15	
corner ov04	35+15	1.08	0.78	10/35	1.23	1.01	0/35	0.71	16.77	1.36	2/15	2.30	0/15	
corner ov05	35+15	0.93	0.43	27/35	1.07	0.58	8/35	0.79	14.60	1.19	3/15	1.90	0/15	
corner ov06	35+15	1.95	0.94	0/35	2.06	0.77	0/35	0.71	27.96	2.00	0/15	3.16	0/15	
corner ov07	35+15	1.05	0.61	6/35	1.16	0.47	3/35	0.74	16.33	1.44	1/15	2.20	0/15	
cube ov00	31+14	0.11	0.03	31/31	0.04	0.15	31/31	0.30	0.70	0.34	14/14	0.49	14/14	
cube ov01	25+12	0.04	0.02	25/25	0.05	0.07	25/25	0.27	0.23	0.29	12/12	0.37	12/12	
cube ov02	24+11	0.06	0.01	24/24	0.04	0.06	24/24	0.28	0.25	0.29	11/11	0.34	11/11	
cube ov03	25+12	0.08	0.04	25/25	0.04	0.14	25/25	0.30	0.44	0.31	12/12	0.38	12/12	
plane 130108MP	35+15	0.09	0.04	35/35	0.32	0.31	32/35	0.47	0.49	0.49	15/15	1.01	9/15	
- plane 2012-A0	30+13	0.65	3.16	0/30	1.43	2.69	0/30	0.56	0.92	0.61	13/13	3.94	0/13	
- plane 3136-H0	19+9	4.17	25.90	0/19	1.50	2.73	0/19	0.95	2.00	1.72	2/9	3.18	0/9	
plane 5501-C4	8+4	1.45	4.42	0/8	1.90	2.52	0/8	0.45	0.15	0.68	3/4	5.37	0/4	
UZH														
DAVIS in45	35+15	0.12	0.18	35/35	0.27	0.56	33/35	0.36	0.14	0.37	15/15	0.43	15/15	
DAVIS inf	35+15	2.08	5.59	18/35	5.03	19.81	0/35	0.50	0.45	0.52	14/15	1.01	10/15	
DAVIS 045	35+15	0.19	0.46	33/35	0.82	2.29	27/35	0.30	0.09	0.30	15/15	0.50	15/15	
DAVIS of	35+15	0.57	1.42	24/35	2.42	10.48	2/35	0.49	0.79	0.49	14/15	0.94	9/15	
Snapdragon in45	35+15	0.12	0.09	35/35	0.33	0.68	31/35	0.26	0.47	0.30	15/15	0.68	14/15	
Snapdragon inf	35+15	0.23	0.32	33/35	0.69	1.79	26/35	0.24	0.82	0.24	15/15	0.42	15/15	
Snapdragon 045	35+15	0.21	0.49	34/35	0.45	0.55	33/35	0.32	0.53	0.33	15/15	0.41	15/15	
paragon 010	22.10	0.00	0.00	05,005	0.05	0.50	20/25	0.01	0.00	0.00	15/15			

Table 4. Complete results for the checkerboard calibration experiment from Section 6.1 in the main paper. The table shows the per-camera results. See the main paper for details on the experimental setup.